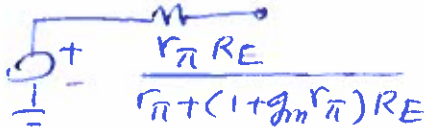


## 215A Diagnostic Test Solutions

①  $\frac{v_{out}}{v_{in}} = -g_m R_L$

②  $\frac{v_{out}}{v_{in}} = \frac{(1+g_m r_{\pi}) R_E}{r_{\pi} + (1+g_m r_{\pi}) R_E}$

③  $\frac{(1+g_m r_{\pi}) R_E}{r_{\pi} + (1+g_m r_{\pi}) R_E} v_{in}$



④  $(\frac{1}{r_{\pi}} + g_m) v_{in}$



⑤  $I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$  If  $V_{TH} \uparrow$ ;  $I_D \downarrow$ .

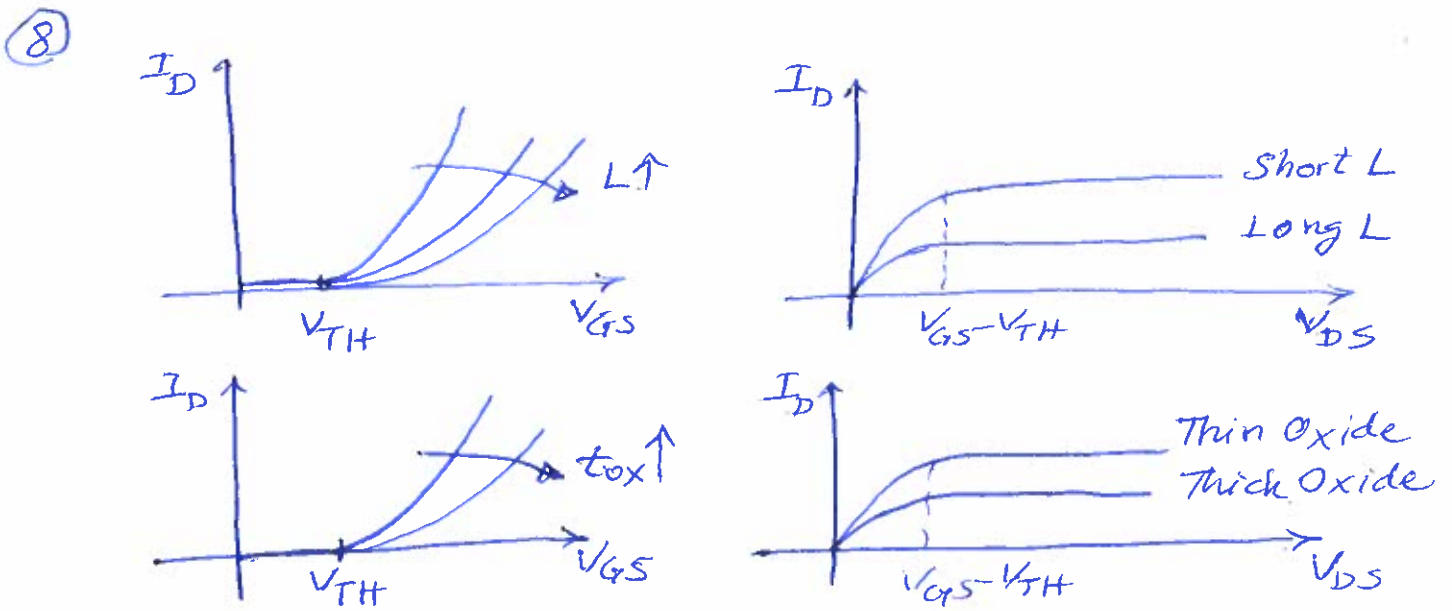
⑥ At low  $V_{DS}$ , the transistor is in the triode region. In this plot, the device is in the deep triode region because  $I_D$  is a linear function of  $V_D$ :

$$I_D = \mu_n C_{ox} \frac{W}{L} \left[ (V_{GS} - V_{TH}) V_{DS} - \frac{V_{DS}^2}{2} \right]$$

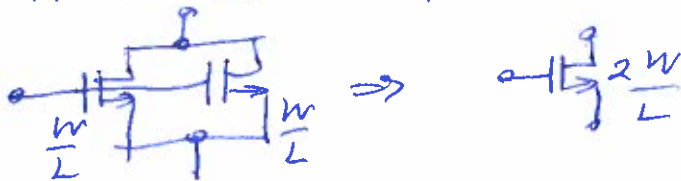
$$\approx \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) V_{DS}$$

$$\Rightarrow \frac{V_{DS}}{I_D} = R_{on} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})}$$

⑦ The device turns on in saturation because  $V_{GS}$  begins to cross  $V_{TH}$  and hence  $V_{GS} - V_{TH}$  is small. That is,  $V_{DS} > V_{GS} - V_{TH}$ .



9) Yes, the two can be lumped into one with twice the width:



10)  $\lambda = 0$  because  $I_D$  is independent of  $V_{DS}$  in the saturation region.

11) We guess that  $M_1$  is in saturation and check at the end -

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (1V - 0.4V)^2 = 200 \mu A$$

$$V_{DS} = V_{DD} - R_D I_D = 0.8V \Rightarrow \text{saturated.}$$

If  $V_{GS}$  changes by 10 mV, the drain current changes by  $g_m \times (10 \text{ mV}) = \mu_n C_{ox} \frac{W}{L} (1V - 0.4V) \times (10 \text{ mV}) = 8.7 \mu A$ , yielding an output voltage change of  $g_m \times (10 \text{ mV}) \times R_D = 33 \text{ mV}$ .

12) At the edge,  $V_{DS} = V_{GS} - V_{TH} = 0.6V \Rightarrow V_{DD} - R_D I_D = 0.6V$   
 $\Rightarrow I_D = 0.24 \text{ mA} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (0.6V)^2 \Rightarrow \frac{W}{L} = 13.3$

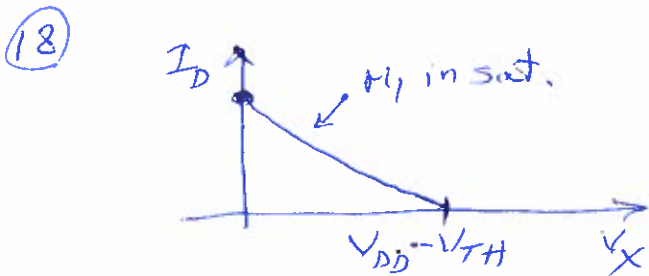
13)  $V_{GS} = V_{DD} - I_D R_D + V_{TH} = V_{DD} + V_{TH} - \frac{R_D}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$   
 $\Rightarrow V_{GS}$  can be found from the quadratic.

14)  $g_m = \sqrt{2 \mu_n C_{ox} \frac{W}{L} I_D} \Rightarrow g_m$  doubles.  $I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$   
 $\Rightarrow V_{GS} - V_{TH}$  const.

15)  $r_o \approx \frac{1}{\lambda I_D} = 10 \text{ k}\Omega$ ,  $\Delta I_D = \frac{\Delta V_{DS}}{r_o} \approx 50 \mu\text{A}$

16) If  $L$  is doubled,  $\lambda$  is halved  $\Rightarrow r_o \approx 20 \text{ k}\Omega \Rightarrow \Delta I_D \approx 25 \mu\text{A}$ .

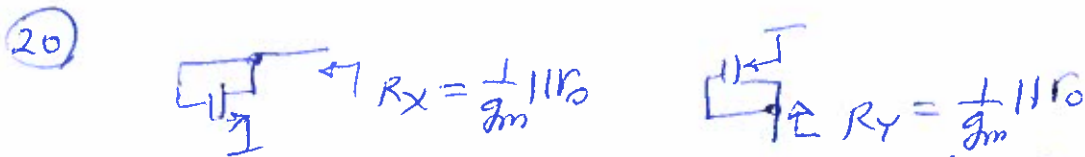
17) Both are right. When using  $g_m = \frac{2I_D}{V_{GS} - V_{TH}}$ , we assume that  $I_D$  is constant and, inevitably,  $W/L$  is variable. For  $g_m = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})$ , on the other hand, we assume  $W/L$  is constant and  $I_D$  is variable.



19) If  $V_{DD} - |V_{TH}| < V_i < V_{DD} \Rightarrow M_1$  is off.

If  $V_i$  falls below  $V_{DD} - |V_{TH}|$ ,  $M_1$  turns on in saturation.

As  $V_i$  falls to  $|V - |V_{TH}|$ ,  $M_1$  reaches the edge of triode region.



Due to the low resistance, these (diode-connected) devices cannot act as current sources.

21) General procedure: (1) determine which terminal is the source (the one with a lower potential), (2) see if the device is on ( $V_{GS} > V_{TH}$ ), and (3) find the region of operation (triode or sat.)

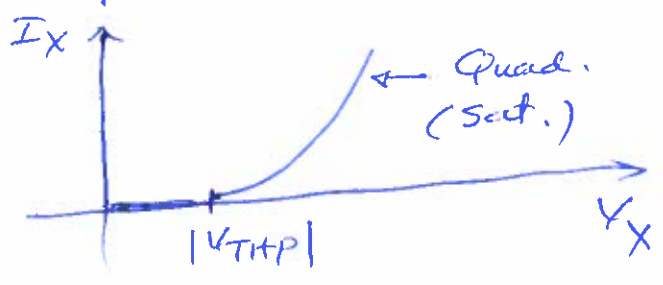
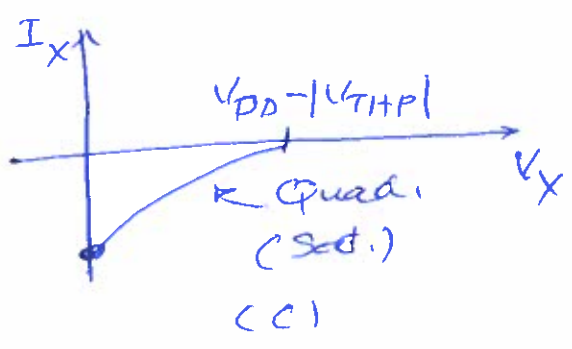
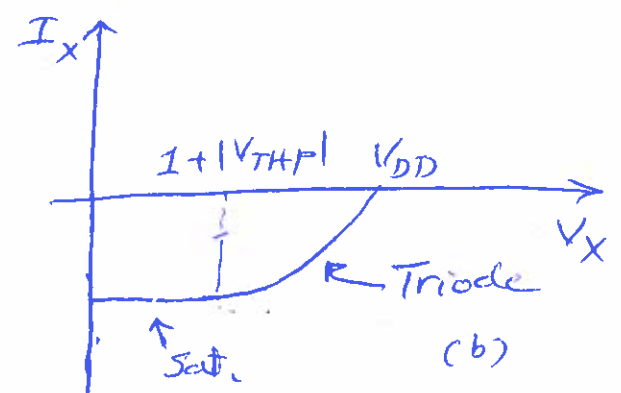
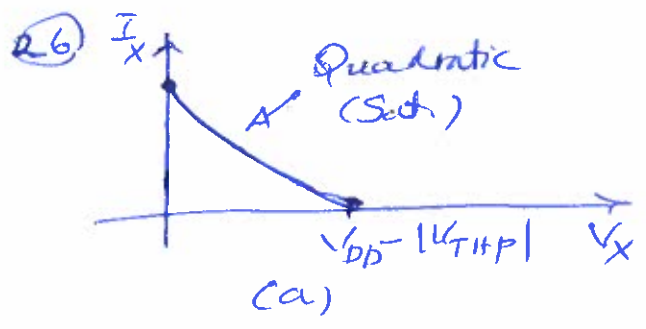
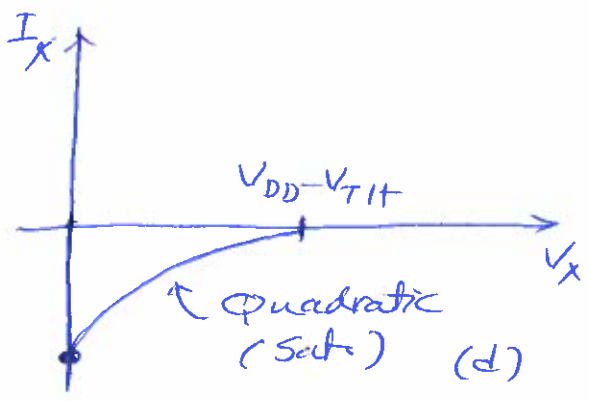
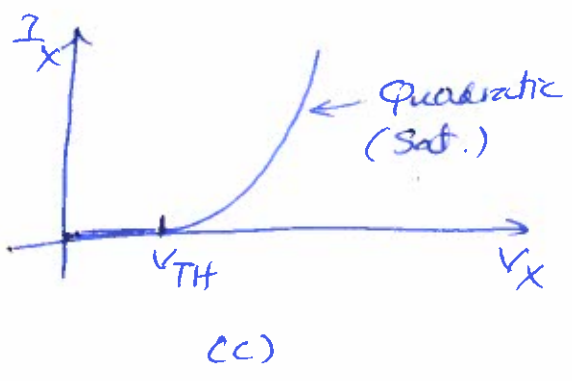
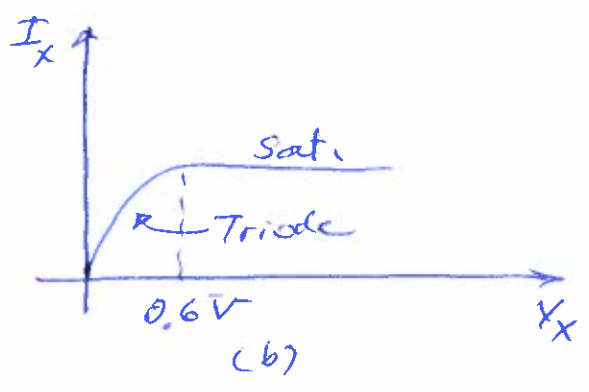
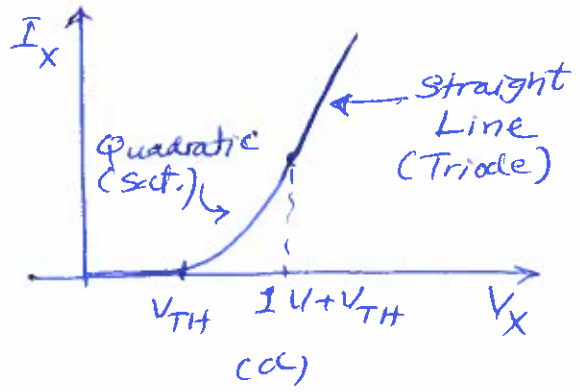
(a) off (b) off (c) triode (d) sat.

22) (a) off (b) sat. (c) triode (d) triode (e) triode (f) off (g) sat. (h) sat. (i) sat.

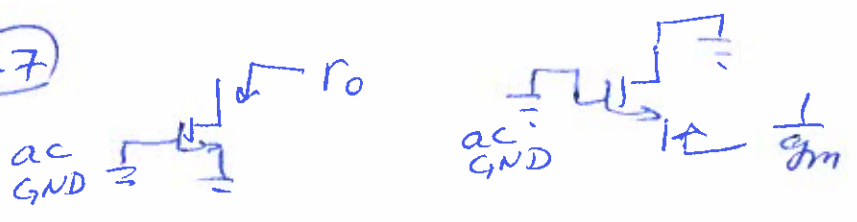
23) (a) off (b) off (c) sat. (d) off

24) (a) sat. (b) triode (c) edge of triode (d) triode

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27



28

The two on the right cannot act as a current source because they exhibit a low output resistance ( $\approx \frac{1}{g_m}$ ).

(29) In a CS stage, the input is applied to the gate and the output is sensed at the drain.

(30)  $A_v = -g_m r_o$  if the current source is ideal.

(31)  $A_v = -g_{m1} (r_{o1} \parallel r_{o2})$

(32)  $A_v = \frac{-R_D}{\frac{1}{g_m} + R_S}$

(33)  $A_v = \frac{-R_D}{\frac{1}{g_{m1}} + \frac{1}{g_{m2}}}$

(34)  $R_{out} = (1 + g_m r_o) R_S + r_o$

(35)  $R_{out} = (1 + g_{m1} r_{o1}) r_{o2} + r_{o1}$

(36) In a CG stage, the input is applied to the source and the output is sensed at the drain.

(37)  $R_{in} = \frac{1}{g_m}$ ,  $R_{out} = R_D$

(38)  $A_v = -g_{m1} (r_{o1} \parallel r_{o2} \parallel \frac{1}{g_{m3}} \parallel r_{o3})$

(39) If  $\lambda = 0$  for all transistors,  $A_v \rightarrow \infty$ .

If  $r_{o2} < \infty$ ,  $A_v = \frac{-r_{o2}}{\frac{1}{g_{m1}} + \frac{1}{g_{m3}}}$

(40)  $\frac{V_{out2}}{V_{in}} = \frac{-\frac{1}{g_{m3}}}{\frac{1}{g_{m1}} + \frac{1}{g_{m2}}}$        $\frac{V_{out1}}{V_{in}} = \frac{\frac{1}{g_{m2}}}{\frac{1}{g_{m1}} + \frac{1}{g_{m2}}}$